

An Improved Dynamic Password based Group Key Agreement against Dictionary Attack

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Abstract—Key exchange protocol is fundamental for establishing secure communication channels over public networks. Password-based key exchange protocols allow parties to share secret key in an authentic manner based on an easily memorizable password. Recently, a password-based group key agreement based on Joux's tripartite key agreement is proposed to improve the performance when users join or leave the group. In this paper, we employ an online dictionary attack on this protocol to show that such kind of modification cannot achieve the basic security of password based group key agreement. With this method, an adversary can test several passwords in one session, which leads the key space reduces greatly to the potential adversaries. To fill the gaps, we propose an improved protocol, which can avoid this attack. Finally, we prove the security of our protocol under the random oracle and ideal cipher model.

Index Terms—Password-based, Group key agreement, Cryptanalysis, Random oracle model, Ideal-cipher model, MDDH

I. INTRODUCTION

The group key agreement [1,2,3] can be regarded as the generalization of two-party key agreement. It allows a group of parties to exchange information among them over an insecure network and agree on a common key. Thereafter, the key can be used to some desirable security services, encryption and data integrity.

Based on the number of the users participating into the key agreement, these protocols are sorted into three kinds: two-party case, three party case, and group case. The first key agreement protocol was proposed by Diffie-Hellman [4] in 1976; it is the two-party case. Then many

papers have extended this two-party protocol to the three-party setting [5] and group setting [6]. However, the Diffie-Hellman protocol and its extensions do not provide the authentication mechanism, and therefore suffer from the man-in-the-middle attack [7] easily. To solve this issue, over the past years, bulks of key agreement protocols [8, 9, 10] with authentication function have been developed.

The password-based key agreement protocols [11,12] require users only to remember a human-memorable low-entropy password, which is rather simple to users. Password-based key agreement protocols are widely used for user authentication and secure communications in real applications, such as internet banking and remote user authentication. The problem of designing a secure password-based key agreement protocol was proposed by Bellare and Merritt [13] in 1992, and has since been studied extensively.

In 2005, Abdalla and Pointcheval [14] proposed a simple two-party password-based authenticated key protocol, which has been proven secure on the basis of the Diffie-Hellman problem. In this scheme, a user, A, sends only one ciphertext, X^* , to B, and B only needs to return one ciphertext, Y^* , to A as well. Then they can work out a common session key, and it is quite simple. The main function of this protocol is equivalent to agree a high-entropy session key with a low-entropy password. However, this protocol cannot be applied to the practical multi-party communications, since it requires each pair of potential communicating parties to share a password. And this leads that a large number of parties result in an even larger number of passwords to be shared. It is due to this

problem, in 2007, Rongxing Lu and Zhenfu Cao [15] proposed a simple three-party password-based key agreement protocol, which is developed from Abdalla and Pointcheval's protocol. In this protocol, each client first shares a human-memorable password with a trusted server, and then when two clients want to agree on a session key, they resort to the trusted server to authenticate each other. This model is more compatible with the Internet.

In 2007, reference [16] proposed a password-based group key agreement based on Joux's tripartite key agreement [17]. In this paper, we make an online dictionary attack on this protocol. With this method, an adversary can test several passwords in one session. Then we propose an improved protocol to fix this gap. Finally, we prove the security of our protocol under the random oracle and ideal cipher model.

II. PRELIMINARIES

A. Bilinear pairing

Let G_1 be a cyclic additive group generated by P , whose order is a prime q , and G_2 be a cyclic multiplicative group with the same order q . A bilinear pairing is a map $e: G_1 \times G_1 \rightarrow G_2$ with the following properties:

1. Bilinearity: $e(aP, bQ) = e(P, Q)^{ab}$ for all $P, Q \in G_1, a, b \in Z_q$.
2. Non-degenerative: There exists $P, Q \in G_1$ such that $e(P, Q) \neq 1$.
3. Computable: There is an efficient algorithm to compute $e(P, Q)$ for all $P, Q \in G_1$.

B. Computational problems

Let G_1 and G_2 be two groups of prime order q , let $e: G_1 \times G_1 \rightarrow G_2$ be a bilinear pairing and let P be a generator of G_1 .

- Discrete Logarithm Problem (DLP)
Let G_1 and G_2 be two groups of prime order q , let $e: G_1 \times G_1 \rightarrow G_2$ be a bilinear pairing and let g be a generator of G_1 . The discrete logarithms (DL) problem can be expressed as follows.

Given $P, g \in G_1$, to find $n \in Z_q$ such that $P = g^n$.

- Decisional Diffie-Hellman problem (DDH)
Let G be a finite cyclic group of prime order q . Given $\Gamma_{real} = \{g, g^x, g^y, g^{xy}\}$ and $\Gamma_{rand} = \{g, g^x, g^y, g^z\}$ where $x, y, z \in Z_q$, it is difficult to distinguish between g^z and g^{xy} . Formally, define the advantage function $Adv_G^{DDH}(\mathcal{A}) = |\Pr[\mathcal{A}(X) = 1] - \Pr[\mathcal{A}(Y) = 1]|$ where $X \in \Gamma_{real}, Y \in \Gamma_{rand}$, we say that the DDH problem is hard in group G if $Adv_G^{DDH}(\mathcal{A})$ is negligible for any probabilistic polynomial time adversary \mathcal{A} . $Adv_G^{DDH}(t)$ is

the maximum value of $Adv_G^{DDH}(\mathcal{A})$ running in time at most t .

- Multi-Decisional Diffie-Hellman problem (MDDH)
Given $\Pi_{real} = \{g, \{g^{x_i}\}_{1 \leq i \leq n}, g^{x_1 \cdot x_2 \cdot \dots \cdot x_n}\}$ and $\Pi_{rand} = \{g, \{g^{x_i}\}_{1 \leq i \leq n}, g^y\}$, where $x_1, \dots, x_n, y \in Z_q$, it is difficult to distinguish between $g^{x_1 \cdot x_2 \cdot \dots \cdot x_n}$ and g^y . Define the advantage function $Adv_G^{MDDH}(\mathcal{A}) = |\Pr[\mathcal{A}(X) = 1] - \Pr[\mathcal{A}(Y) = 1]|$, where $X \in \Gamma_{real}, Y \in \Gamma_{rand}$, the DDH problem is hard in group G if $Adv_G^{MDDH}(\mathcal{A})$ is negligible for any probabilistic polynomial time adversary \mathcal{A} . $Adv_G^{MDDH}(t)$ is the maximum value of $Adv_G^{MDDH}(\mathcal{A})$ running in time at most t .

C. Security definitions

In 2005, reference [12, 14] proposed the real-or-random (ROR) model instead of the find-and-guess model of Bellare and Rogaway [18] to prove a three-party password-based authenticated key exchange protocol. This model seems more suitable for the password-based setting and we shall prove our scheme under this model.

A player may have numerous instances, called oracles, of distinct concurrent executions of the protocol. We denote the j -th instance of U_i by U_i^j . The interaction between the adversary \mathcal{A} and players occurs only via oracle queries, which describe the capabilities of \mathcal{A} . In the ROR model, Reveal queries are replaced by Test queries; Execute queries are introduced to model passive attack and can easily be simulated with the Send queries. The Send query and Test query are described as follows:

Send (U_i^j, m): This query models an active attack. \mathcal{A} can intercept a message and then either modify it or create a new one to the intended player. The output of this query is the response generated by the instance U_i^j upon receipt of the message m according to the execution of protocol P . The adversary can initiate the execution of P by sending a query ($U_i^j, start$).

Test (U_i^j): This query models the indistinguishability of the real session key from a random string. Once the instance U_i^j has accepted a session key, the adversary can attempt to distinguish it from a random key as the basis of determining security of the protocol. A random bit b is chosen and if $b=1$ then the real session key is returned while if $b=0$ then a random key is returned. Adversary outputs a guess bit b' . If $b' = b$, where b is the hidden bit used by U_i^j , \mathcal{A} wins the game.

III. THE PROPOSED IMPROVED DYNAMIC PASSWORD SCHEME

A. Review of the original protocol

The algorithm for odd users is different from that for even users in reference [16]. Since the even-user

algorithm is based on the odd-user one, they firstly describe the odd-user algorithm. Assume that the system pre-distributes a common password pw for each user. There exists a secure cipher scheme (E, D) , where E is an encrypt algorithm, and D is the matching decrypt algorithm. $H : \{0,1\}^* \rightarrow \{0,1\}^l$ is a hash function to generate the encryption key. The basic scheme for odd-user is as follows:

Step1. The user $U_i \in \{U_1, \dots, U_n\}$ computes the key $k_i = H(U_i \parallel pw \parallel i)$, choose $x_i \in Z_q^*$ randomly, computes $X_i = g^{x_i}$, and then sends $X_i^* = E_{k_i}(X_i)$ to his neighbors $U_{i-2}, U_{i-1}, U_{i+1}, U_{i+2}$. Assume $U_{n+1} = U_1$, $U_{n+2} = U_2$, and $Q = e(g, g)$.

Step2. After receiving X_j^* , the user U_i computes $k_j = H(U_j \parallel pw \parallel j)$ and $X_j = D_{k_j}(X_j^*)$, and then computes U_i^R and U_i^L respectively.

$$\begin{aligned} U_1^R &= e(X_2, X_3)^{x_1} = Q^{x_1 x_2 x_3}, \\ U_1^L &= e(X_{n-1}, X_n)^{x_1} = Q^{x_{n-1} x_n x_1}, \\ &\dots, \\ U_i^R &= e(X_{i+1}, X_{i+2})^{x_i} = Q^{x_i x_{i+1} x_{i+2}}, \\ U_i^L &= e(X_{i-2}, X_{i-1})^{x_i} = Q^{x_{i-2} x_{i-1} x_i}, \\ &\dots, \\ U_n^R &= e(X_1, X_2) = Q^{x_1 x_2 x_n}, \\ U_n^L &= e(X_{n-2}, X_{n-1})^{x_n} = Q^{x_{n-2} x_{n-1} x_n} \end{aligned}$$

Step3. The user U_i computes $K_i = U_i^R / U_i^L$ and broadcasts the value to all the members in the group over the Internet. After this phase, the user U_i should have the following values

$$\begin{aligned} K_1 &= U_1^R / U_1^L = Q^{x_1 x_2 x_3 - x_{n-1} x_n x_1}, \\ &\dots, \\ K_i &= U_i^R / U_i^L = Q^{x_i x_{i+1} x_{i+2} - x_{i-2} x_{i-1} x_i}, \\ &\dots, \\ K_n &= U_n^R / U_n^L = Q^{x_n x_1 x_2 - x_{n-2} x_{n-1} x_n} \end{aligned}$$

Step4. Before computing a common session key, the user U_i should verify the values got from other group members. Since $U_i^R = U_{i+2}^L$, the user U_i can compute as follows

$$\begin{aligned} U_{i+2}^R &= K_{i+2} \cdot U_{i+2}^L = K_{i+2} \cdot U_{i+2}^R, \\ &\dots, \\ U_i^L &= U_{i-2}^R = K_{i-2} \cdot U_{i-2}^L \end{aligned}$$

and verify the equation

$$U_i^L \stackrel{?}{=} U_i^L$$

If the above equation holds, the values that U_i gets from his neighbors are correct. Otherwise, stop the protocol and output error message.

Step5. When the user U_i decides the above steps are finished, he will compute each U_i^R . Since $U_i^R = U_{i+2}^L$,

each user can compute $U_{i+2}^R = K_{i+2} \cdot U_i^R$. Then the common session key is computed.

$$sk_{odd} = U_1^R U_2^R \dots U_n^R$$

In the case of even users, the users should implement the following additional steps.

Step6. Suppose that there exists a user set $\{U_1, U_2, \dots, U_n, U_{n+1}\}$ and the user $\{U_1, U_2, \dots, U_n\}$ have negotiated a common session key by above steps. User $\{U_1, U_n\}$ send X_1^* and X_n^* to U_{n+1} respectively. User U_{n+1} computes the key $k_{n+1} = H(U_{n+1} \parallel pw \parallel n+1)$, chooses $x_{n+1} \in Z_q^*$ uniformly at random, computes $X_{n+1} = g^{x_{n+1}}$, and then sends $X_{n+1}^* = E_{k_{n+1}}(X_{n+1})$ to U_1 and U_n . Upon receiving X_{n+1}^* , users $\{U_1, U_n\}$ compute k_{n+1} and $X_{n+1} = D_{k_{n+1}}(X_{n+1}^*)$ respectively. Then the users U_1, U_n and U_{n+1} compute $Z_{n+1} = Q^{x_1 x_n x_{n+1}}$ as their temporary session key.

Step7. The users U_1, U_n encrypt the common session key Z_{n+1} using sk_{odd} as the secret key, and broadcast the corresponding ciphertext to other user. Thereby, any user who obtains the session key Z_{n+1} and sk_{odd} can compute the updated session key

$$sk = H(sk_{odd}, Z_{n+1}).$$

Thereafter, users U_1 and U_n encrypt sk using Z_{n+1} as the secret key, and send the corresponding ciphertext to user U_{n+1} . After implementing above steps, all the users share the updated common session key sk .

B. Cryptanalysis of the original protocol

Since our online dictionary attack is for the basic odd-user protocol, the other part of their protocol is left out of this paper. Meanwhile, the attacking process is similar with the even user setting.

The attack is described as follows. Let k be the number of honest players. The adversary starts a session in which all the honest players have indices of the form $3(i-1)+3$ for $i=1, \dots, k$. The adversary plays the role of player $3(i-1)+1$ and $3(i-1)+5$. we also assume $U_{n+1} = U_1$. There are $3k$ players in all. Then, let $\{pw_1, \dots, pw_m\}$ be a list of candidate passwords that an adversary wants to try. The adversary gets out k candidate passwords to test in this message.

1. He computes $k_{3(i-1)+1} = H(U_{3(i-1)+1} \parallel pw_i \parallel 3(i-1)+1)$ and $k_{3(i-1)+5} = H(U_{3(i-1)+5} \parallel pw_i \parallel 3(i-1)+5)$, $i=1, \dots, k$. Then he chooses $x_1, x_5, \dots, x_{3(k-1)+1}, x_{3(k-1)+5} \in Z_q$, computes corresponding $X_i = g^{x_i}$, and broadcasts $X_i^* = E_{k_i}(X_i)$.

2. He decrypt $X_{3(i-1)+1} = D_{k_{3(i-1)+1}}(X_{3(i-1)+1}^*)$ and $X_{3(i-1)+5} = D_{k_{3(i-1)+5}}(X_{3(i-1)+5}^*)$ with the guessed pw_i , tests whether $z_{3(i-1)+5}^L / z_{3(i-1)+1}^R = K_{3(i-1)+3}$ hold.

Therefore, the Adversary can test k candidate passwords from the list with one session.

C. the proposed password based group key agreement protocol

Assume that the system pre-distributes a common password pw for each player and $U_{n+1} = U_1$. There exists a secure cipher scheme (E,D), where E is an encrypt algorithm. $H : \{0,1\}^* \rightarrow \{0,1\}^{l_H}$ is a hash function to generate the encryption key and $H_1 : \{0,1\}^* \rightarrow \{0,1\}^{l_{H_1}}$ is a hash function to update the session key. e is a bilinear pairing, $Q = e(g, g)$ is public.

Step 1. The player $U_i \in \{U_1, \dots, U_n\}$ computes the key $k_i = H(U_i \parallel pw \parallel i)$, choose $x_i \in \mathbb{Z}_q^*$ randomly, computes $X_i = g^{x_i}$, and then sends $X_i^* = E_{k_i}(X_i \parallel k_i)$ to his neighbors $U_{i-2}, U_{i-1}, U_{i+1}, U_{i+2}$.

Step 2. After receiving X_j^* , the player U_i computes $k_j = H(U_j \parallel pw \parallel j)$ and decrypts $X_j \parallel k_j = D_{k_j}(X_j^*)$ with it. Then he check whether the k_j decrypted from X_j^* is identical to the k_j computed from pw and the user index j. After this verification, he computes $U_i^L = e(X_{i-2}, X_{i-1})^{x_i} = Q^{x_i \cdot x_{i-1} \cdot x_{i-2}}$, $U_i^R = e(X_{i+1}, X_{i+2})^{x_i} = Q^{x_i \cdot x_{i+1} \cdot x_{i+2}}$, $K_i = U_i^R / U_i^L$ and broadcast K_i to all the members in the group over the network.

Step 3. Since $U_i^R = U_{i+2}^L$, U_i computes $U_{i+2}^R = K_{i+2} U_i^R$ and gets all U_i^R s. Then he computes the session key $sk = U_1^R U_2^R \dots U_n^R$ if n is an odd number. If n is an even number, the Steps4 and Step5 are with the same function as the Step 6 and Step 7 of the original protocol.

Step 4. Suppose that there exists a user set $\{U_1, U_2, \dots, U_n, U_{n+1}\}$ and the user $\{U_1, U_2, \dots, U_n\}$ have negotiated a common session key by above steps. User $\{U_1, U_n\}$ send X_1^* and X_n^* to U_{n+1} respectively. User U_{n+1} computes the key $k_{n+1} = H(U_{n+1} \parallel pw \parallel n+1)$, chooses $x_{n+1} \in \mathbb{Z}_q^*$ uniformly at random, computes $X_{n+1} = g^{x_{n+1}}$, and then sends $X_{n+1}^* = E_{k_{n+1}}(X_{n+1} \parallel k_{n+1})$ to U_1 and U_n . Upon receiving X_{n+1}^* , users $\{U_1, U_n\}$ compute k_{n+1} and $X_{n+1} \parallel k_{n+1} = D_{k_{n+1}}(X_{n+1}^*)$ respectively. Then they check whether the two k_{n+1} are identical. Finally, the users U_1, U_n and U_{n+1} compute $Z_{n+1} = Q^{x_1 x_n x_{n+1}}$ as their temporary session key if the two k_{n+1} are identical.

Step 5. The users U_1, U_n encrypt the common session key Z_{n+1} using sk_{odd} as the secret key, and broadcast the corresponding ciphertext to other users. Thereby, any user who obtains the session key Z_{n+1} and sk_{odd} can compute the updated session key

$$sk = H_1(sk_{odd}, Z_{n+1}).$$

Thereafter, users U_1 and U_n encrypt sk using Z_{n+1} as the secret key, and send the corresponding ciphertext to user U_{n+1} . After above steps, all the users share the updated common session key sk.

IV. SECURITY ANALYSIS OF OUR IMPROVED PROTOCOL

The following Theorem 1 presents the main security result of the proposed password-based group key agreement protocol

Theorem 1. Let P denote the proposed protocol in which the password is chosen in a dictionary of size N. For any adversary \mathcal{A} running in time t, that makes at most q_{active} attempts within at most $q_{session}$ sessions, his advantage in breaking the semantic security of the session key, in the ideal-cipher model, is upper-bounded by:

$$\begin{aligned} Adv_P^{ror-aka}(\mathcal{A}) &\leq 2q_D q_H + 2q_H^2 / 2^{l_H} + 2q_{H_1}^2 / 2^{l_{H_1}} \\ &+ 2nq_{session} q_E + 2q_{H_1} + (q_E + q_D)^2 / |G| \\ &+ 2 \frac{nq_{session} Adv_G^{ddh}(t) + q_{H_1} / |G| + q_{active} / N}{2^{l_H}} \\ &+ 2nq_{session} Adv_G^{ddh}(t) \end{aligned}$$

where q_H, q_{H_1}, q_E, q_D denote the number of oracle queries the adversary is allowed to make to the random oracles H and H_1 , and to the ideal-cipher oracles E and D, respectively.

This theorem shows the advantage of the adversary essentially grows linearly with the number of active attempts that the adversary makes and the passive attacks are essentially negligible because an honest transcript does not help a computationally bounded adversary in guessing the password.

Proof. We incrementally define a sequence of games from the game Game0 to Game7. In each game, various adversary behaviors are simulated and the advantages of an adversary \mathcal{A} are upper-bounded. At the end of the games, we measure the probability $|\Pr[Suc_i] - \Pr[Suc_{i-1}]|$ between Game_i and Game_{i-1}. Finally, we get the result of the Theorem 1 by using the difference of the probability.

Game0. This experiment simulates the real attack. The advantage of \mathcal{A} in this protocol is defined as $Adv_P^{ror-aka}(\mathcal{A}) = 2 \Pr[Suc_0] - 1$

Game1. In this game, we simulate the random oracles H and H_1 by maintaining the list L_H and L_{H_1} , respectively.

If \mathcal{A} asks a H query of the form (U_i, i, pw) such that a record (U_i, i, pw, r) exists in the list L_H , then r is returned. Otherwise, r is chosen randomly from $\{0,1\}^{l_H}$, and (U_i, i, pw, r) is recorded to L_H . Define the collision event in the output of H by Col_H . Then the probability of that bad event is upper-bounded by $q_H^2 / 2^{l_H}$. Similarly, the probability of the collision event Col_{H_1} in the output

of H_1 is upper-bounded by $q_{H_1}^2/2^{l_{H_1}}$. Game0 and Game1 are perfectly indistinguishable unless that the bad events Col_H and Col_{H_1} occur simultaneously. Thus, we have

$$|\Pr[Suc_1] - \Pr[Suc_0]| \leq q_H^2/2^{l_H} + q_{H_1}^2/2^{l_{H_1}}.$$

Game2. This game simulates the ideal-cipher oracles E and D by maintaining a list $L_{E,D}$, which keeps track of the previous queries-answers and links each query to a specific player. $L_{E,D}$ has the form $(U_i, i, e, \text{type}, k, X, X^*)$, where $\text{type} \in \{\text{enc}, \text{dec}\}$. Such record means that $X^* = \mathcal{E}_k(X \| k)$, and type indicates which kind of queries generated the record. The index i indicates which player is associated with the key k , while U_i indicates the user. These values are all set to null if k does not come from a H query of the form $(U_i, i, *)$ with $i \in \{1, \dots, n\}$. The e will be explained in the next game. E and D can be simulated as follows:

Encryption query: For an encryption query $\mathcal{E}_k(X \| k)$, if a record $(\cdot, \cdot, \cdot, \cdot, k, X, *)$ exists in the list $L_{E,D}$, the element $*$ is returned. Otherwise, a random value $X^* \in G$ is returned and $(\text{null}, \text{null}, \text{null}, \text{enc}, k, X, X^*)$ is added into $L_{E,D}$.

Decryption query: For a decryption query $D_k(X^*)$, if a record $(\cdot, \cdot, \cdot, \cdot, k, *, X^*)$ exists in the list $L_{E,D}$, the element $*$ is returned. Otherwise, if k has been returned to a hash query of the form $(U_i, i, *)$, we choose X randomly in $G \setminus \{0\}$ and update the list $L_{E,D}$ with $(U_i, i, \cdot, \text{dec}, k, X, X^*)$; otherwise, we choose X randomly in $G \setminus \{0\}$ and update the list $L_{E,D}$ with $(\cdot, \cdot, \cdot, \text{dec}, k, X, X^*)$. Finally, X and is returned.

The above simulation is perfect, except for the following two bad events. First, collisions may appear that contradict the permutation property of the ideal-cipher. The probability can be upper-bounded by $(q_E + q_D)^2/2|G|$. Second, in the case of the decryption query simulation, one will abort executions if the value k involved in a decryption query is output by H. The probability is at most $q_H/2^{l_H}$ for each decryption query. For any k involved in a decryption query, if k comes from an H query, we know the corresponding pair (U_i, i) . Thus, we have

$$|\Pr[Suc_2] - \Pr[Suc_1]| \leq (q_E + q_D)^2/2|G| + q_D q_H/2^{l_H}$$

Game3. In this game, we change the simulation of the decryption queries, and make use of our challenger to embed an instance of the MDDH problem in the protocol simulation. Let the challenger output tuples $(\gamma_1, \gamma_2, \dots, \gamma_n, \lambda_1, \lambda_2, \dots, \lambda_n)$. We use these tuples to properly simulate the decryption queries. More precisely, we make a new tuple each time a new session appears in a decryption query. However, if several queries are asked with the same session, the challenger outputs the same tuple.

Given a tuple outputted by the challenger, for any randomly chosen (e_1, e_2, \dots, e_n) , the tuple $(\gamma_1^{e_1}, \gamma_2^{e_2}, \dots, \gamma_n^{e_n}, \lambda_1^{e_1 e_2}, \lambda_2^{e_2 e_3}, \dots, \lambda_n^{e_n e_1})$ has the same distribution as the original tuple. We make this property as follows, by modifying the sub-case previously considered for new decryption queries in the Game3.

Decryption query: For a decryption query $D_k(X^*)$ such that $k = H(U_i, i, *)$ was previously obtained from H for some valid index i , we query challenger for getting a tuple $(\gamma_1, \gamma_2, \dots, \gamma_n, \lambda_1, \lambda_2, \dots, \lambda_n)$. Then we choose $e \in \mathbb{Z}_q^*$ randomly, add the record $(U_i, i, e, \text{dec}, k, X = \gamma^e, X^*)$ into the list $L_{E,D}$, and return X .

The list $L_{E,D}$ whose records are of the form $(U_i, i, e, \text{type}, k, X, X^*)$ has been defined. Above change of simulation on the decryption queries does not modify the view of the adversary. So:

$$\Pr[Suc_3] = \Pr[Suc_2]$$

Game4. In this game, we simulate the Send query in the first and the second round. When the session starts, player i computes the symmetric keys as $k_j = H(U_j, j, pw)$, for all player j . Thus, we are working with the tuple $(\gamma_1, \gamma_2, \dots, \gamma_n, \lambda_1, \lambda_2, \dots, \lambda_n)$.

In the Step1, U_i randomly chooses a value $X_i^* \in G$ to be broadcasted, and asks $D_{k_i}(X_i^*)$ with the simulation in Game3. The simulation leads to add e_i to the list $L_{E,D}$, unless X_i^* already appeared as an encryption result. But the latter event can not happen with probability greater than $q_E/|G|$.

In the Step2, U_i recovers all $X_j \| k_j = D_{k_j}(X_j^*)$, and checks whether $k_j = H(U_j, j, pw)$. If X_j^* has been simulated according to the above simulation of the Step1, one gets e_{i-1} and e_{i+1} in the list $L_{E,D}$ such that $X_j = \gamma_j^{e_j}$. Otherwise, one of the X_j^* has been previously answered by the encryption oracle in response to an attacker query $E_k(X \| k)$, where $k = H(U_j, j, pw)$ is the correct key for player U_j . We denote such an event by Encrypt. In such a case, the simulation is terminated and the adversary wins. Thus, one gets $X_{i-2} = \gamma_{i-2}^{e_{i-2}}$, $X_{i-1} = \gamma_{i-1}^{e_{i-1}}$, $X_i = \gamma_i^{e_i}$, $X_{i+1} = \gamma_{i+1}^{e_{i+1}}$, $X_{i+2} = \gamma_{i+2}^{e_{i+2}}$ correctly computes $U_i^L = \lambda_{i-1}^{e_{i-2} e_{i-1} e_i}$, $U_i^R = \lambda_i^{e_{i-2} e_i e_{i+1}}$, then broadcasts $K_i = U_i^R / U_i^L$. After this round, each player can compute the session key as before. The simulation is still perfect, unless the above bad events happen. Therefore, we get $|\Pr[Suc_4] - \Pr[Suc_3]| \leq q_{\text{passive}} \cdot q_E/|G| + \Pr[\text{Encrypt}_1]/2^{l_H} \leq nq_{\text{session}} q_E/|G| + \Pr[\text{Encrypt}_1]/2^{l_H}$

Game5. Since it is clear that the security of the above protocol still relies on the DDH assumption, let the

challenger output
 tuples $(\gamma_1, \gamma_2, \dots, \gamma_n, \lambda_1, \lambda_2, \dots, \lambda_n)$ according to the Π_{rand}
 distribution. We have

$$|\Pr[Suc_5] - \Pr[Suc_4]| \leq q_{\text{ession}} Adv_G^{mddh}(t) \leq n q_{\text{ession}} Adv_G^{ddh}(t)$$

$$\begin{aligned} |\Pr[Encrypt_2] - \Pr[Encrypt_1]| &\leq q_{\text{ession}} Adv_G^{mddh}(t) \\ &\leq n q_{\text{ession}} Adv_G^{ddh}(t) \end{aligned}$$

Game6. Since the session key is computed from U_i^R and K_i , the collision has been upper-bounded by above games. In this game, we derive the session keys using a private random oracle $H_1 : sk = H_1(sk_{\text{odd}}, Z_{n+1})$ to simulate the updated session key. After the modification of the derivation of the session key, the probability for the adversary to see the difference between the current and the previous games is to query $H_1 : sk = H_1(sk_{\text{odd}}, Z_{n+1})$. From the previous game, we know no information has been leaked about sk and these queries are identical inside each session: the probability of such an event can also be upper-bounded by $q_G / |G|$. Thus, we have

$$\begin{aligned} |\Pr[Suc_6] - \Pr[Suc_5]| &\leq q_{H_1} / |G| \\ |\Pr[Encrypt_3] - \Pr[Encrypt_2]| &\leq q_{H_1} / |G| \end{aligned}$$

Since the private oracle \mathcal{G} is private to the simulator, it is clear that

$$\Pr[Suc_6] = 1/2.$$

Game7. One can note that the password pw is only used in the simulation of the first and second rounds to compute k_i with the element γ_i . But only K_i which is computed from λ_{i-1} and λ_i is outputted. In this game, we can simplify the simulation of the second and third rounds as follows: In the first round, U_i randomly chooses $X_i^* \in G$, and sends it with no decryption. In the second round, U_i simply computes and sends $K_i = \lambda_i / \lambda_{i-1}$. This simulation is perfect since one does not need anymore to compute the session key. Thus, the probability of the Encrypt event is less than the number of first flows manufactured by the adversary. We have

$$\Pr[Encrypt_3] \leq q_{\text{active}} / N$$

In the above, the collisions in the output have been eliminated in previous games and we can get the Theorem 1.

V. CONCLUSION

Password-based group key agreement is an important research field in key agreement protocol and plays an outstanding role in distributed networks. In this paper, we make an online dictionary attack on this protocol. With this method, an adversary can test several passwords in one session. Then we propose an improved protocol to fix this gap. Finally, we prove the security of our protocol under the random oracle and ideal cipher model.

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“Registration and private key distribution protocol based on IBE”, the 5th International Conference on Frontier of Computer Science and Technology-FCST2010, Changchun, China, 2010.

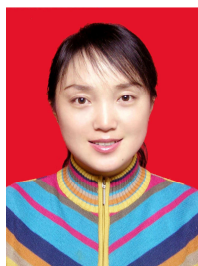
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An important objective of the projects is to probe the trend of network security, which can satisfy the need of constructing high-speed, large-scale and multi-services networks. Various complex attacks can not be dealt with by simple defense. And to add mechanisms to network architecture results in decreasing performance. In a word, fundamental re-examination of how to build trustworthy distributed network should be made.



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